

Numerical Modeling

(Separate notes accompany this PowerPoint)

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Outline

- Numerical Models
- NWP
- WRF

What are numerical models?

A numerical model numerically integrates a set equations for a volume of the atmosphere, which is divided into a series of material volumes, called the grid mesh.

“Model” of the atmosphere

- Take equations that describe atmospheric processes
- Convert them into a form where they can be programmed into a computer
- Solve the equations so that this software representation of the atmosphere evolves within the computer
- This is called a “model” of the atmosphere

Example of solving equation

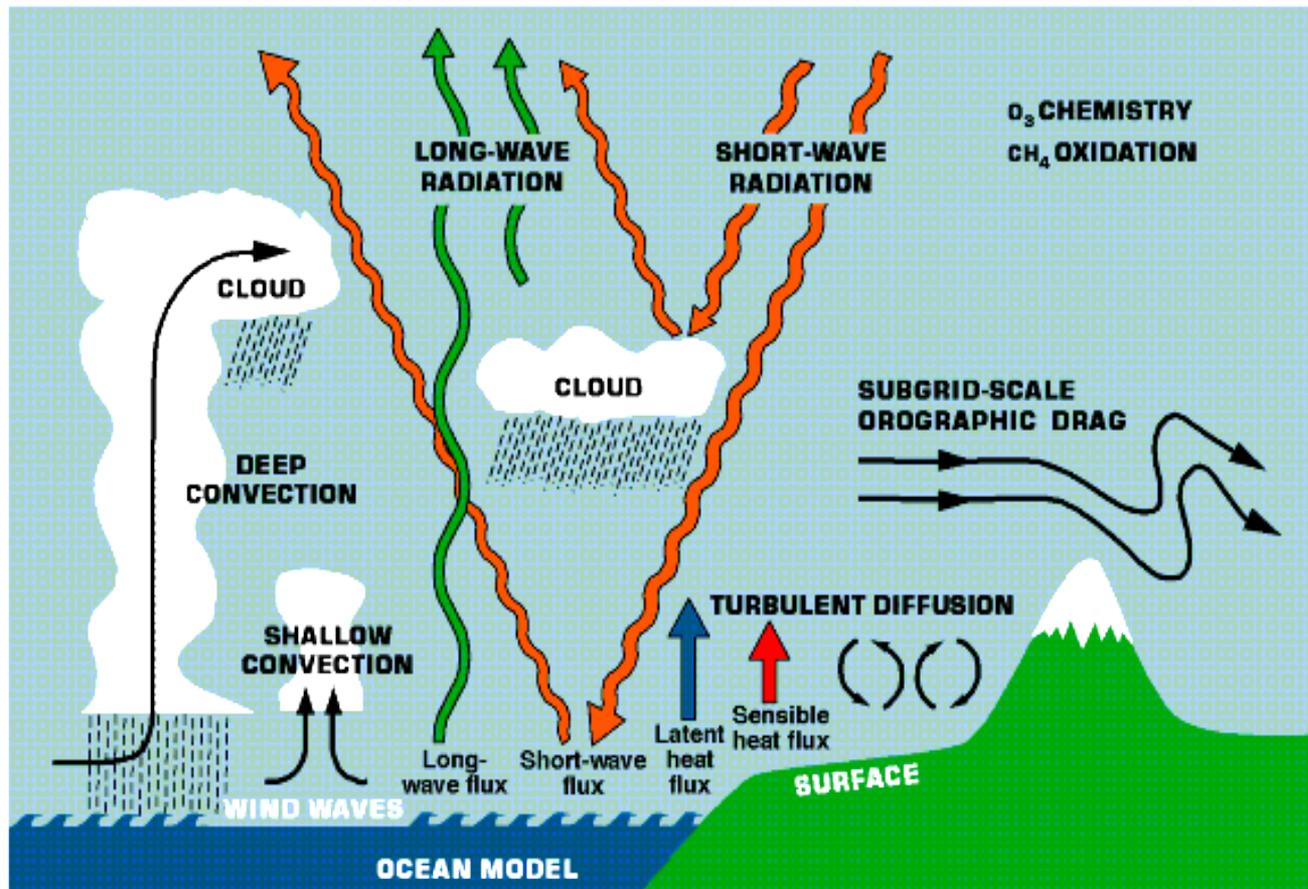
- $$\frac{T_{\{change\}}}{time} = solar + IR (gain) + IR (loss) + conduction + convection + evaporation + condensation + advection$$

So – “solving” the equation implies estimating the terms on the right hand side, adding them up and obtaining rate of change of temperature.

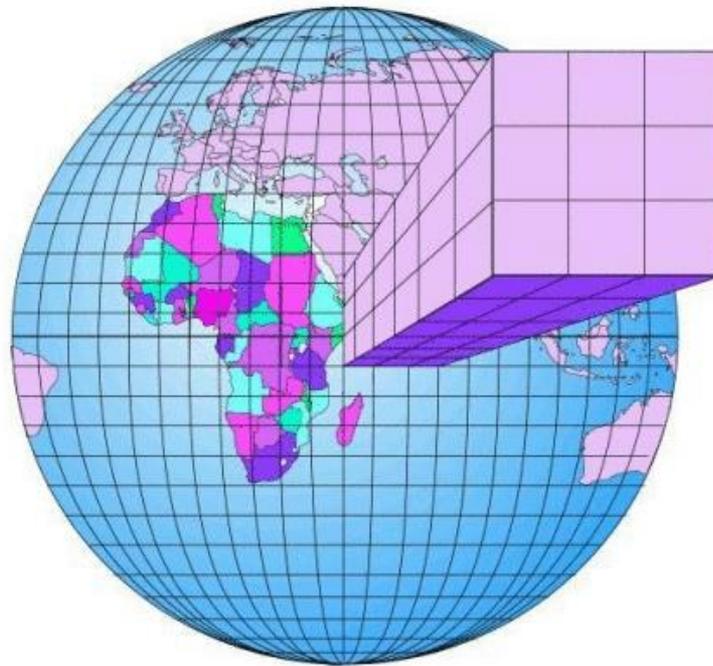
Similar Equations are solved for

- East-west wind component
- North-south wind component
- Specific humidity (or RH)
- Pressure
- Cloud water
- Rain/snow water

Schematic of processes that generally require parameterization



Low resolution grid mesh for a global model

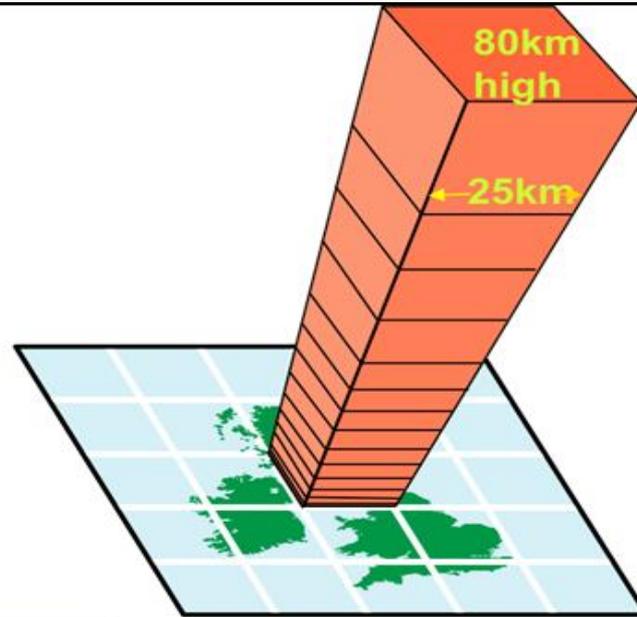
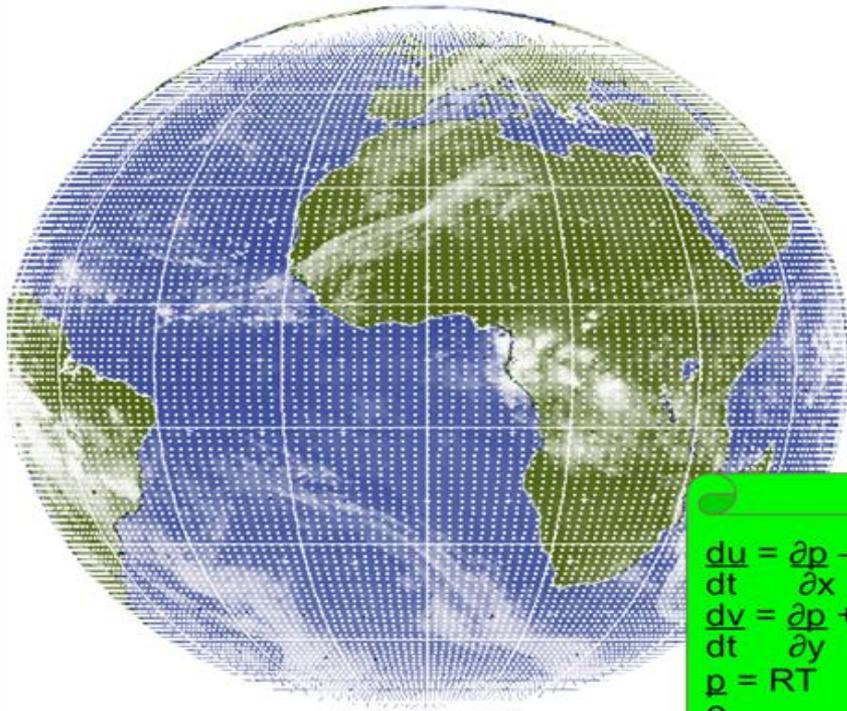


Some Basics

- Matter of interest (e.g. atmosphere) is assumed to be continuous
- Modeling material volume
- Material volume has bulk properties of density, temperature, velocity, etc

Putting the ideas in perspective

Pressure, Temperature, winds, moisture



$$\frac{du}{dt} = \frac{\partial p}{\partial x} - fv$$
$$\frac{dv}{dt} = \frac{\partial p}{\partial y} + fu$$
$$p = RT$$
$$\rho$$

Newton's laws for rotating fluid

Gas laws

Laws of thermodynamics

Figure 10.5: Model horizontal and vertical grids on the sphere used to solve the fluid equations to provide a numerical weather forecast. The dimensions and grid spacings are from the Met Office Unified Model (MetUM) used for global NWP (Circa August 2013).

Two Types of Models

- Global – grid covers the entire atmosphere of Earth (global models)
- Limited area – grid covers a region of the atmosphere such as continent, sub-continent or city (limited area models).

Types of Models

- Global Climate Models (GCMs)
- Regional Models/Limited Area Models (LAMs) or Mesoscale Models
- Cloud Resolving Models (CRM)

Element's of a model(1)

- The basic coordinate system
 - Longitude, latitude, sigma, time
- Meteorological variables
 - Wind, temperature, pressure, moisture content, etc at every level at each grid point
- The governing equations

Governing Equations

- Conservation of momentum (Newton's laws)
 - 3 equations for accelerations of 3-d wind ($F = Ma$)
- Conservation of mass
 - 1 equation for conservation of air (mass continuity)
 - 1 equation for conservation of water
- Conservation of energy
 - 1 equation for the first law of thermodynamics
- Relationship among ρ , V , and T
 - 1 equation of state (ideal gas law)

Elements of a model (2)

- Physical processes
 - Boundary conditions (Lower, Upper, Lateral)
 - Surface Characteristics (Topography, Land-Sea)
 - Horizontal Diffusion
 - Boundary Layer
 - Heat Transfer Processes
 - Moisture and Precipitation

Uses of Atmospheric Models

- Daily weather prediction (models are allowed to run into the future for 1-10 days)
- Climate prediction (models are allowed to run for years
 - “what if” experiments, e.g. what will happen if we double CO₂?
 - Simply let the model run forward
- Research – You can study the model solution when you do not have good observations of real atmosphere

What is NWP (1)?

A method of weather forecasting that employs:

- A set of equations that describe the flow of fluids,
- Which is translated into computer code,
- Combined with parameterizations of other processes,
- Then applied on a specific domain,
- And integrated, based on initial conditions and conditions at the domains' boundaries

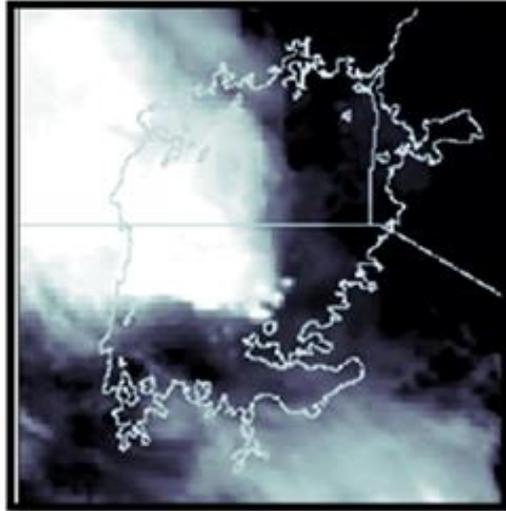
What is NWP (2)?

A method of weather forecasting that employs:

- Governing equations
- Numerical methods
 - Finite difference (based on Taylor series)
 - Finite volume (based on fluxes in and out of volume)
 - Spectral (calculated in Fourier space)
- Parameterizations
- Domains
- Initial and boundary conditions

(a) SATELLITE

IR 04/03/2012 0300 UTC



(b) NWP MODELS

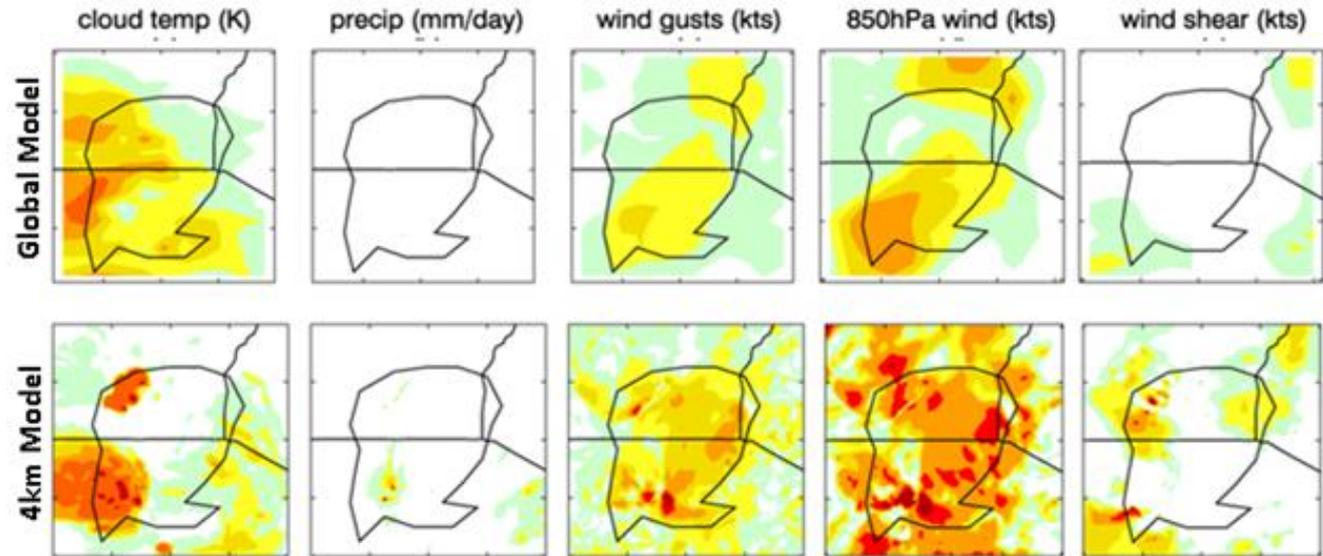


Figure 10.22: Case Study of Lake Victoria storm from 4th March 2012: (a) Satellite IR imagery (b) Met Office NWP operational model performance for Global and 4 km models. (Reproduced from Fig. 7, 8 and 9 of Chamberlain et al. (2013))

Source: The Forecasters' Handbook chp 10

Introduction to WRF Model

- Weather Research and Forecasting Model
- Different WRF Models with same architecture but different core codes
 - ARW (Advanced Research WRF) at NCAR
 - NMM (Non-Hydrostatic Mesoscale Model) at NCEP
 - Based on Eta Model's code

Architecture of WRF Model

DRIVER

- *Manages execution over nested grids*
- *Controls input/output*
- *Top-level control over parallel processing*

MEDIATOR

- *Makes calls to parallel mechanisms*

MODEL

- *Contains numerics and physics*
- *Performs model computations*

Suitability

- Idealized simulations (e.g. LES, convection, baroclinic waves)
- Parameterization research
- Data assimilation research
- Forecast research
- Real-time NWP
- Coupled-model applications
- Teaching
- Climate Simulation

Grand Vision for WRF Model

- From the start, WRF was intended to be used for both research and operations
 - Shorten time between research developments in NWP and application to operations
 - Increase communication and understanding between research and operational communities

Platforms for WRF Model

- Can be run on a variety of platforms: single processor, shared or distributed memory

Remarks

- The WRF Model is state-of-the-art in operational mesoscale NWP, free, has a large user community sharing knowledge, has a technical support team at NCAR
- WRF Tutorial presentations in PPT and PDF
<http://www.mmm.ucar.edu/wrf/users/supports/tutorial.html>
- WRF technical paper
<http://www.mmm.ucar.edu/wrf/users/pub-doc.html>

Thank you

Extras

Numerics in WRF Model

- The WRF Model's numerics are higher order than MM5's, so they contain more terms and better approximate the governing equations
 - Horizontal advection: 5th order
 - Vertical advection: 3rd order
 - Temporal integration: 3rd order

Domains

Three domains
2-way nested

DX=
40.5/13.5/4.5 km

Dimensions

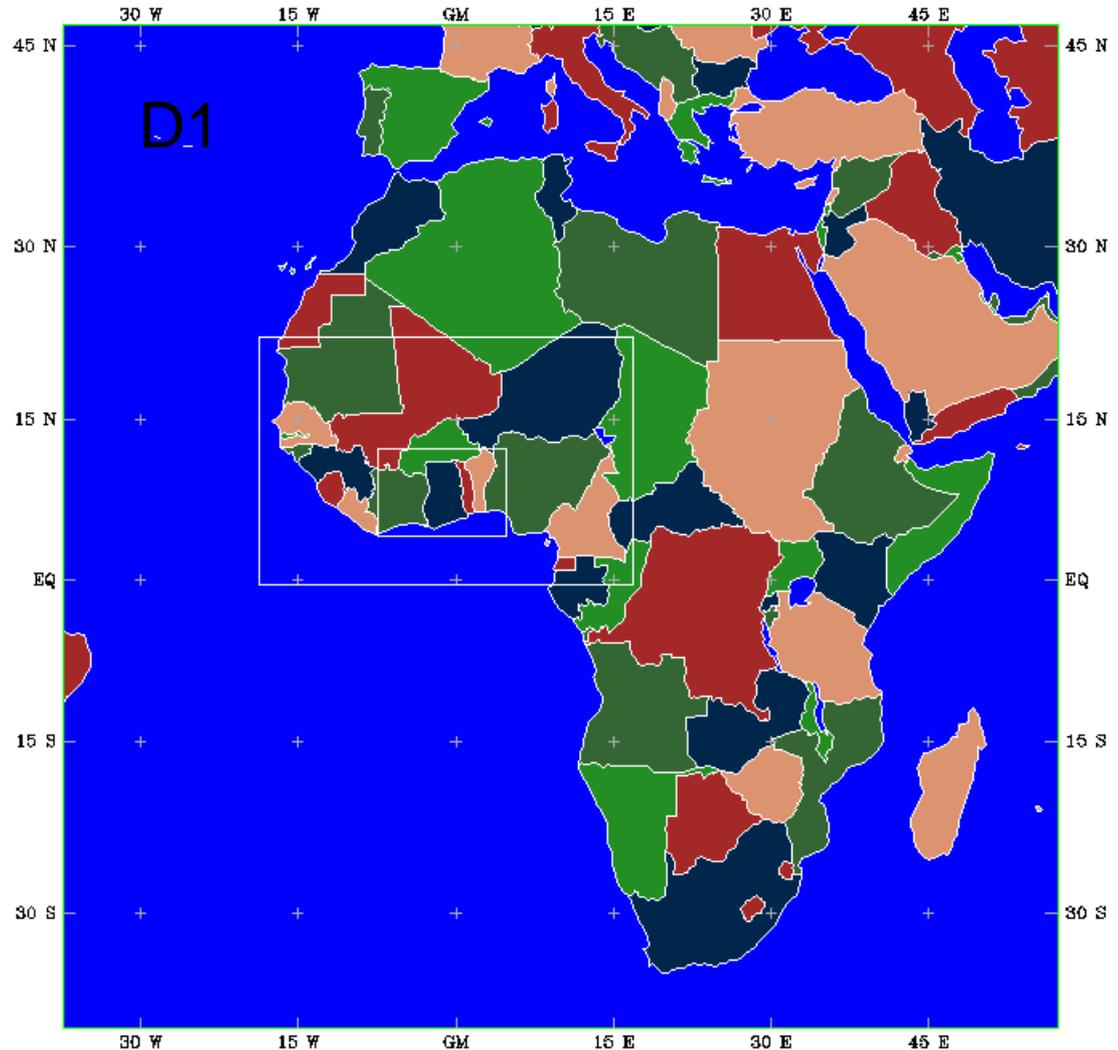
D1: 261x261x36

D2: 184x295x36

D3: 208x301x36

D1 is largest domain

D3 is smallest domain



Governing Equations

Higher order advection schemes, which lead to a higher effective resolution than in many other NWP models

- Almost every model uses a slightly different set of equations.
- Why?
 - Application to different parts of the world
 - Focus on different atmospheric processes
 - Application to different time and spatial scales
 - Ambiguity and uncertainty in formulations
 - Tailoring to different uses

Governing Equations

- The WRF Model is one of the first cloud-scale models designed to conserve mass, momentum, and energy.
- But...
 - Water is only perfectly conserved if positive definite advection (available since V2.2) is used
 - Momentum and energy are not numerically conserved
 - Momentum is not really conserved because it is a staggered variable, and so can't use the mass conservation property accurately

ARW Solver (1)

- **Equations:** Fully compressible, Euler nonhydrostatic with a run-time hydrostatic option available. Conservative for scalar variables.
- **Prognostic Variables:** Velocity components u and v in Cartesian coordinate, vertical velocity w , perturbation potential temperature, perturbation geopotential, and perturbation surface pressure of dry air. Optionally, turbulent kinetic energy and any number of scalars such as water vapor mixing ratio, rain/snow mixing ratio, and cloud water/ice mixing ratio.
- **Vertical Coordinate:** Terrain-following hydrostatic-pressure, with vertical grid stretching permitted. Top of the model is a constant pressure surface.
- **Horizontal Grid:** Arakawa C-grid staggering.
- **Time Integration:** Time-split integration using a 3rd order Runge-Kutta scheme with smaller time step for acoustic and gravity-wave modes.
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ARW Solver (2)

- **Initial Conditions:** Three dimensional for real-data, and one-, two- and three-dimensional using idealized data. A number of test cases are provided.
- **Lateral Boundary Conditions:** Periodic, open, symmetric, and specified options available.
- **Top Boundary Conditions:** Gravity wave absorbing (diffusion or Rayleigh damping). $w = 0$ top boundary condition at constant pressure level.
- **Bottom Boundary Conditions:** Physical or free-slip.

ARW Solver (3)

- **Spatial Discretization:** 2nd to 6th order advection options in horizontal and vertical.
- **Turbulent Mixing and Model Filters:** Sub-grid scale turbulence formulation in both coordinate and physical space. Divergence damping, external-mode filtering, vertically implicit acoustic step off-centering. Explicit filter option also available.
- **Earth's Rotation:** Full Coriolis terms included.
- **Mapping to Sphere:** Three map projections are supported for real-data simulation: polar stereographic, Lambert-conformal, and Mercator. Curvature terms included.
- **Nesting:** One-way, two-way, and moving nests

Model Physics

- **Microphysics: Bulk schemes ranging from simplified physics suitable for mesoscale modeling to sophisticated mixed-phase physics suitable for cloud-resolving modeling.**
- **Cumulus parameterizations: Adjustment and mass-flux schemes for mesoscale modeling including NWP.**
- **Surface physics: Multi-layer land surface models ranging from a simple thermal model to full vegetation and soil moisture models, including snow cover and sea ice.**
- **Planetary boundary layer physics: Turbulent kinetic energy prediction or non-local K schemes.**
- **Atmospheric radiation physics: Longwave and shortwave schemes with multiple spectral bands and a simple shortwave scheme. Cloud effects and surface fluxes are included**